

# Question Bank

Subject : Mathematics Paper II sem VI ( Numerical Method)

## Unit I

- 1) Find the root, correct to the three decimal places & lying between 2&3 of the equation  $X^3 - 2x^2 - 5$  By using Bisection Method.
- 2) Find the root, correct to the three decimal places & lying between 2&3 of the equation  $X^3 - 2x^2 - 5$  By using regula falsi Method.
- 3) By Using Newton Raphson Method to find a real root of  $x \sin x + \cos x = 0$  near  $x = \pi$  iteration upto 4 decimal places.
- 4) Given  $\frac{dy}{dx} = 1 + y^2$  where  $y(0) = 0$ . Find  $y(0.2)$  &  $y(0.4)$  by Runge kutta fourth order formula.
- 5) Find the root, correct to the three decimal places & lying between 2&3 of the equation  $X^3 - x - 1$  By using Bisection Method.
- 6) Find the root, correct to the three decimal places & lying between 2&3 of the equation  $X^3 - x - 1$  By using falsi position Method.
- 7) Find the root of the equation  $X^3 - 2x - 5 = 0$  By using secant Method.
- 8) Find the root of the equation  $X^3 - x - 1 = 0$  By using secant Method.

## Unit II

- 1) 3) Using Newton Forward differential formula .find the sum  $s_n = 1^3 + 2^3 + 3^3 + \dots$
- 2) Find the cubic polynomial which takes the following values  $y(1)=24$ ,  $y(3)=120$ ,  $y(5)=336$ ,  $y(7)=720$ . Hence, or otherwise obtain the value of  $y(8)$
- 3) Value of  $x$  (in degree) and  $\sin x$  are given in following table.

| X in degree | Sin x     |
|-------------|-----------|
| 15          | 0.2588190 |
| 20          | 0.3420201 |
| 25          | 0.4226183 |
| 30          | 0.5       |
| 35          | 0.5735764 |
| 40          | 0.6427876 |

Determine the value of  $\sin 38^\circ$  by using Newton's Backward Difference Formula.

4) The table below gives the value of  $\tan x$  for  $0.10 \leq x \leq 0.30$

| X    | Y= tan x |
|------|----------|
| 0.10 | 0.1003   |
| 0.15 | 0.1511   |
| 0.20 | 0.027    |
| 0.25 | 0.2553   |
| 0.30 | 0.3093   |

find  $\tan (0.12)$  ,  $\tan (0.30)$

5) For the following table, find the value of  $e^{1.17}$  using Gauss forward formula.

| X    | Y= e <sup>x</sup> |
|------|-------------------|
| 1.00 | 2.7183            |
| 1.05 | 2.8577            |
| 1.10 | 3.0042            |
| 1.15 | 3.1582            |
| 1.20 | 3.3201            |
| 1.25 | 3.4903            |
| 1.30 | 3.6693            |

6) The following table gives the value of  $e^x$  for a certain equidistant values of  $x$  and find the value of  $e^x$  for  $x=0.644$ . using stirling and Bessel's Formula.

| $x$  | $Y=e^x$  |
|------|----------|
| 0.61 | 1.840431 |
| 0.62 | 1.858928 |
| 0.63 | 1.877610 |
| 0.64 | 1.896481 |
| 0.65 | 1.915541 |
| 0.66 | 1.934792 |
| 0.67 | 1.954237 |

7) Certain corresponding value of  $x$  and  $\log x$  are (300,2.4771),(304,2.4829)&(307,2.4871). Find  $\log 301$ .

## Unit III

1) from the following table of values of  $x$  &  $y$  .obtain  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$  for  $x = 1, 2$

| $x$ | $y$    |
|-----|--------|
| 1.0 | 2.7183 |
| 1.2 | 3.3201 |
| 1.4 | 4.0552 |
| 1.6 | 4.9530 |
| 1.8 | 6.0496 |
| 2.0 | 7.3891 |
| 2.2 | 9.0250 |

2) Calculate 1<sup>st</sup> and 2<sup>nd</sup> derivatives of the function tabulated in the previous table at the point  $x=2.2$  and also  $\frac{dy}{dx}$  at  $x=2.0$

| $x$ | $y$    |
|-----|--------|
| 1.0 | 2.7183 |
| 1.2 | 3.3201 |
| 1.4 | 4.0552 |
| 1.6 | 4.9530 |
| 1.8 | 6.0496 |
| 2.0 | 7.3891 |
| 2.2 | 9.0250 |

3) Find  $\frac{dy}{dx}$  and  $\frac{d^2y}{dx^2}$  at  $x=1.6$  for the tabulated function

| x   | y      |
|-----|--------|
| 1.0 | 2.7183 |
| 1.2 | 3.3201 |
| 1.4 | 4.0552 |
| 1.6 | 4.9530 |
| 1.8 | 6.0496 |
| 2.0 | 7.3891 |
| 2.2 | 9.0250 |

4) Find the area bounded by the curve and the x-axis from  $x=7.47$  to  $x=7.52$

| x    | F(x) |
|------|------|
| 7.47 | 1.93 |
| 7.48 | 1.95 |
| 7.49 | 1.98 |
| 7.50 | 2.01 |
| 7.51 | 2.03 |
| 7.52 | 2.06 |

5) Evaluate  $I = \int_0^1 \frac{1}{1+x} dx$  correct to three decimal places by trapezoidal and Simpson's rule with  $h = 0.5, 0.25, 0.125$  resp.

6) Use the Euler-Maclaurin formula to prove,  $\sum x^2 = \frac{n(n+1)(n+2)}{6}$

## Unit IV

1) Given that differential equation  $y'' - xy' - y = 0$ . With the condition  $y(0)=1$  &  $y'(0) = 0$  use Taylor's series method to determine the value of  $y(0.1)$  correct to the seven decimal places.

2) Use of Picard's method to obtain  $y^{(1)}$  and  $y^{(2)}$ . Solve the equation  $y' = x + y^2$ , subject to the constraint  $y=1$  when  $x=0$  & find  $y^{(2)}$ .

3) Determine the value of  $y$  when  $x=0.1$  given that  $y(0)=1$  &  $y' = x^2 + y^2$  by modified Euler's method take  $h=0.05$

4) Given,  $\frac{dy}{dx} = 1 + y^2$  where  $y(0) = 0$ . Find  $y(0.2)$  and  $y(0.4)$  by Runge-Kutta fourth order formula.

